

## SEQUENCES

Page	Description
1	Write and complete sequences by adding or taking a number
2	Introduce the nth term rule for sequences
3	Term to term rule and the nth term rule
4	Recap on linear sequences
5	Special sequences. Squares, cubes, triangular numbers, Fibonacci and Geometric sequences
6	Introduction to quadratic sequences
7	Find the nth term of a quadratic sequence

# Sequences

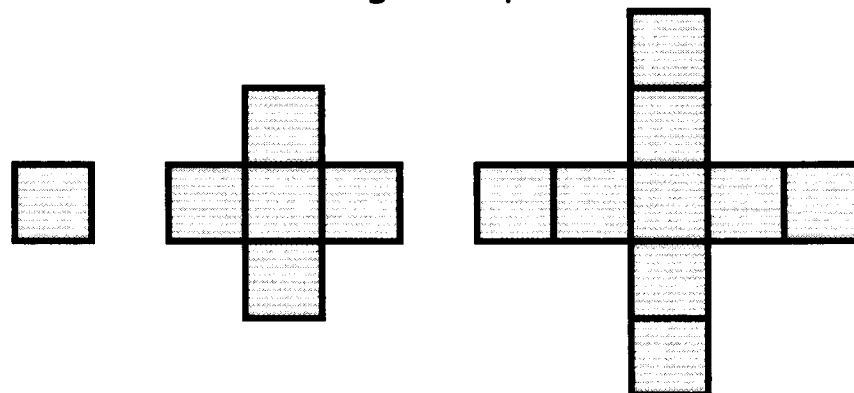
Write down the first FIVE numbers in each of these sequences.

- 1) The sequences starts with 7. The rule is add 2.
- 2) The sequences starts with 8. The rule is add 6.
- 3) The sequences starts with 3. The rule is add 7.
- 4) The sequences starts with 20. The rule is take 3.
- 5) The sequences starts with 15. The rule is take 4.

Write down the next two terms of these sequences and their rule.

- 6) 8, 12, 16, 20. \_\_\_\_, \_\_\_\_ The rule is
- 7) 5, 12, 19, 26. \_\_\_\_, \_\_\_\_ The rule is
- 8) 2.5, 3.5, 4.5, 5.5. \_\_\_\_, \_\_\_\_ The rule is
- 9) 21, 19, 17, 15. \_\_\_\_, \_\_\_\_ The rule is
- 10) 24, 17, 10, 3 \_\_\_\_, \_\_\_\_ The rule is

Use these drawings for questions 11 to 14



- 11) Write down the sequence from the drawings. \_\_\_\_, \_\_\_\_, \_\_\_\_, \_\_\_\_, \_\_\_\_
- 12) What is the rule for the sequence?
- 13) What is the tenth number in this sequence?
- 14) The number 25 is the sequence. Which term is it?

Use these drawings for questions 15 to 18



- 15) Write down the sequence from the drawings. \_\_\_\_, \_\_\_\_, \_\_\_\_, \_\_\_\_, \_\_\_\_
- 16) What is the rule for the sequence?
- 17) What is the tenth number in this sequence?
- 18) The number 17 is the sequence. Which term is it?

# Sequences

Qu. 1  $n^{\text{th}}$  term rule  **$3n + 1$**

3 x the position + 1

position	1st term	2nd term	3rd term	4th term	5th term	10th term
	$n = 1$	$n = 2$	$n = 3$	$n = 4$	$n = 5$	$n = 10$
term	$3 \times \mathbf{1} + 1$	$3 \times \mathbf{2} + 1$	$3 \times \mathbf{3} + 1$	$3 \times \mathbf{4} + 1$	$3 \times \mathbf{5} + 1$	$3 \times \mathbf{10} + 1$

term to  
term rule

Qu. 2  $n^{\text{th}}$  term rule  **$4n - 1$**

4 x the position - 1

position	1st term	2nd term	3rd term	4th term	5th term	10th term
	$n = 1$	$n = 2$	$n = 3$	$n = 4$	$n = 5$	$n = 10$
term	$4 \times \mathbf{1} - 1$	$4 \times \mathbf{2} - 1$	$4 \times \mathbf{3} - 1$	$4 \times \mathbf{4} - 1$	$4 \times \mathbf{5} - 1$	$4 \times \mathbf{10} - 1$

term to  
term rule

Qu. 3  $n^{\text{th}}$  term rule  **$2n + 3$**

2 x the position + 3

position	1st term	2nd term	3rd term	4th term	5th term	10th term
	$n = 1$	$n = 2$	$n = 3$	$n = 4$	$n = 5$	$n = 10$
term	$2 \times \underline{\quad} + 3$	$2 \times \underline{\quad} + 3$	$2 \times \underline{\quad} + 3$	$2 \times \underline{\quad} + 3$	$2 \times \underline{\quad} + 3$	$2 \times \underline{\quad} + 3$

term to  
term rule

Qu. 4  $n^{\text{th}}$  term rule  **$5n - 2$**

5 x the position - 2

position	1st term	2nd term	3rd term	4th term	5th term	10th term
	$n = 1$	$n = 2$	$n = 3$	$n = 4$	$n = 5$	$n = 10$
term	$5 \times \underline{\quad} - 2$	$5 \times \underline{\quad} - 2$	$5 \times \underline{\quad} - 2$	$5 \times \underline{\quad} - 2$	$5 \times \underline{\quad} - 2$	$5 \times \underline{\quad} - 2$

term to  
term rule

Qu. 5  $n^{\text{th}}$  term rule  **$4n + 3$**

4 x the position + 3

position	1st term	2nd term	3rd term	4th term	5th term	10th term
	$n = 1$	$n = 2$	$n = 3$	$n = 4$	$n = 5$	$n = 10$
term						

term to  
term rule

Qu. 6  $n^{\text{th}}$  term rule  **$24 - 2n$**

24 - 2 x the position

Remember !!  
Times before take

position	1st term	2nd term	3rd term	4th term	5th term	10th term
	$n = 1$	$n = 2$	$n = 3$	$n = 4$	$n = 5$	$n = 10$
term	$24 - 2 \times \mathbf{1}$	$24 - 2 \times \mathbf{2}$				
	$24 - 2$	$24 - 4$				
	22	20				

term to  
term rule

**1** 4, 9, 14, 19.....

The term to term rule is

The nth term rule is

The 20th term is

**2** 20, 16, 12, 8 .....

The term to term rule is

The nth term rule is

The 20th term is

**3** The rule for a sequence is  $2n - 3$ .

Write down the first five terms of the sequence.

What is the 20th term of this sequence?

Is 64 in this sequence?

**4** 7, 11, 15, 19 .....

The term to term rule is

The nth term rule is

The 20th term is

**5** The rule for a sequence is  $4n + 3$ .

Write down the first five terms of the sequence.

What is the 20th term of this sequence?

Is 64 in this sequence?

**6** The rule for a sequence is  $24 - 2n$ .

Write down the first five terms of the sequence.

What is the 20th term of this sequence?

Is -64 in this sequence?

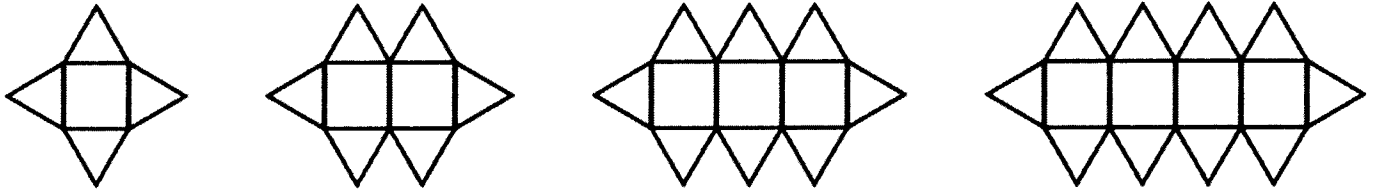
## Sequences

Write down the first FIVE terms and the 10<sup>th</sup> for each of these sequences.

- 1)  $4n + 3$
- 2)  $2n + 7$
- 3)  $10 - n$
- 4)  $24 - 2n$
- 5)  $3n - 2$

Write down the "by position" or nth term rule for these sequences.

- 6) 3, 5, 7, 9, 11
- 7) 6, 10, 14, 18, 22
- 8) 2, 5, 8, 11, 14
- 9) 21, 19, 17, 15, 13
- 10) 30, 27, 24, 21, 18
- 11)



Pattern number (n)	1	2	3	4	5	6
Squares	1	2	3	4	5	6
Triangles	4	6	8	10	12	14

Find the rule for the number of triangles given the pattern number (n)

How many triangles in the 20<sup>th</sup> drawing?

12) Here are the first five terms of a sequence.

**8 11 14 17 20**

Work out the 11th term of the sequence. Explain how you worked out your answer.

④

# Complete the sequences

SQUARE NUMBERS

1, 4, 9, 16, —, —, —, —, —

$1^2 = 1$   
 $2^2 = 4$   
 $3^2 = 9$

CUBE NUMBERS

1, 8, 27, —, —, —, —, —, —

$1^3 = 1$   
 $2^3 = 8$   
 $3^3 = 27$

TRIANGULAR NUMBERS

1, 3, 6, 10, —, —, —, —, —

1    3    6    10

Fibonacci    Add the last two terms to make the next one. For example 1, 1, 2, 3, 5, —, —, —, —

Geometric Sequence    One term is multiplied by a fixed number to make the next term. E.g. 1, 2, 4, 8, 16, 32, —

Write down the first FIVE terms for these Quadratic Sequences

$$n^2 + 2n + 1$$

$$2n^2 - 3$$

$$n^2 - 3n + 4$$

Find the nth term rule for this quadratic sequence 2, 6, 12, 20, 30

⑥

Find the rules  
for these quadratic  
sequences.

Qu. 1

n	1	2	3	4	5
term	2	8	16	26	38

Qu. 2

n	1	2	3	4	5
term	7	17	31	49	71

Qu. 3

n	1	2	3	4	5
term	9	17	31	51	77

Qu. 4

n	1	2	3	4	5
term	8	30	62	104	156

Qu. 5

n	1	2	3	4	5
term	6	24	52	90	138

Qu. 6

n	1	2	3	4	5
term	11	15	15	11	3

Qu. 7

n	1	2	3	4	5
term	12	26	44	66	92

Qu. 8

n	1	2	3	4	5
term	3	6	13	24	39

Qu. 9

n	1	2	3	4	5
term	6	17	34	57	86