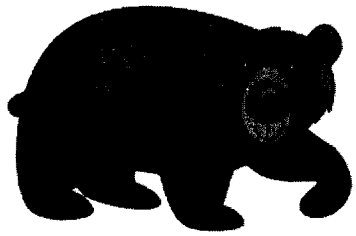


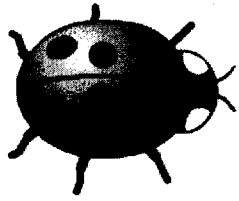
## AVERAGES

Page	Description
1	Collect the data then find the mode, median, mean and range. Odd number of pieces of data
2	Collect the data then find the mode, median, mean and range. Even number of pieces of data
3	Find mean, median, mode and range of ages of students in two schools. Compare the results
4	Find mean, median, mode and range of sets of data including a frequency table
5	Find mean, median, mode and range from a frequency table
6	Find mean, median, mode and range from a grouped frequency table
7	Averages review



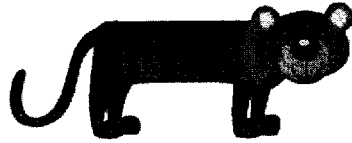
Animal Bear

Legs 4



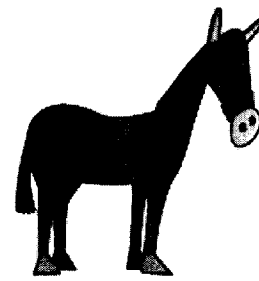
Animal Ladybird

Legs 6



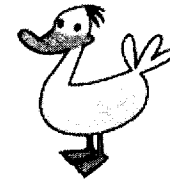
Animal Tiger

Legs 4



Animal horse

Legs 4



Animal duck

Legs 2

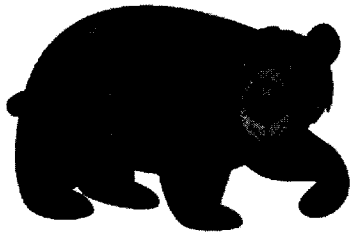
Mode 4 legs

Median 2, 4, 4, 4, 6 4 legs

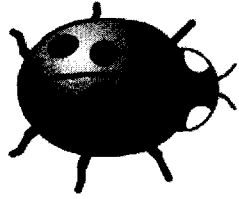
Mean  $\frac{2 + 4 + 4 + 4 + 6}{5} = \frac{20}{5} = 4$  legs

Range  $6 - 2 = 4$  legs

# LEGS



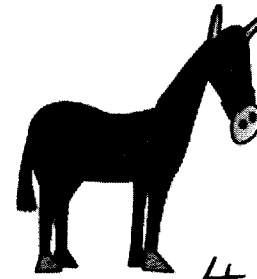
4



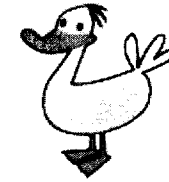
6



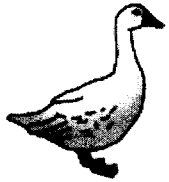
4



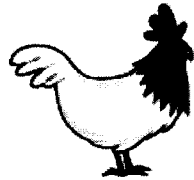
4



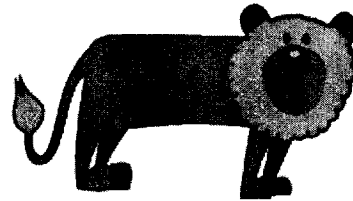
2



2



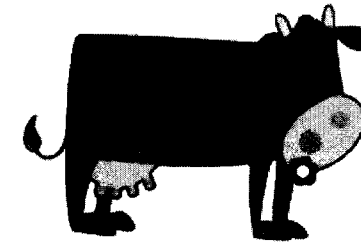
2



4



4



4

## The data

Write down the number of legs each animals has

2, 2, 2, 4, 4, 4, 4, 4, 4, 6

## Find

The mean

$$\frac{36}{10} = 3.6 \text{ legs}$$

The mode

4 legs

The median

$$\frac{4+4}{2} = 4 \text{ legs}$$

The range

$$6 - 2 = 4.$$

(2)

The data shows the age in years of a group of students and teachers within each school.

School A                      student total = 180                      adult total = 187

students      7 7 7 8 8 8 9 9 10 10 10 10 11 11 11 11 11 11 11

teachers      24 29 34 42 58

19  
5  
—  
24

School B                      student total = 250                      adult total = 221

students      11 11 11 11 12 12 13 14 14 14 14 15 15 16 16 16 17 18

teachers      26 29 31 38 44 53

18  
6  
—  
24

- 1) Which school is a Primary School? **A**
- 2) Which school is a Secondary School? **B**
- 3) What is the age of the youngest student in School A? **7**
- 4) What is the range of ages of students in School A?  $11 - 7 = 4$
- 5) What is the range of ages of students in School B?  $18 - 11 = 7$
- 6) What is the median age of the teachers in School A? **34**
- 7) What is the median age of the teachers in School B?  $\frac{31 + 38}{2} = \frac{69}{2} = 34.5$
- 8) Which school has the oldest teacher? **A**
- 9) What is the median age of the group from School A?  $\frac{10 + 11}{2} = 10.5$
- 10) What is the median age of the group from School B?  $\frac{15 + 15}{2} = 15$
- 11) What is the age of the youngest teacher in School B? **26**
- 12) Calculate the mean age of the students  $180 + 250 = 430$        $19 + 18 = 37$   
 $430 \div 37 = 11.6$

	Mean	Mode	Median	Range
School A students	$\frac{180}{19} = 9.5$	11	10	4
School A teachers	$\frac{187}{5} = 37.4$	X	34	34
School A whole group	$\frac{367}{24} = 15.3$	11	10.5	51

	Mean	Mode	Median	Range
School B students	$\frac{250}{18} = 13.9$	11 and 14	14	7
School B teachers	$\frac{221}{6} = 36.8$	X	34.5	27
School B whole group	$\frac{471}{24} = 19.6$	11 and 14	15	42

## Mean, Median, Mode and Range

Find the mean, median, mode and range of these sets of numbers.

- 1) 4 6 8 8 10      Mean =  $36 \div 5 = 7.2$     Med = 8    mode = 8    Range = 6
- 2) 3 2 1 3 3      Mean =  $12 \div 5 = 2.4$     Med = 3    mode = 3    R = 2
- 3) 7 6 7 2 3 1 9    Mean =  $35 \div 7 = 5$     Med = 6    mode = 7    R = 8
- 4) 6 6 9      Mean =  $21 \div 3 = 7$     Med = 6    mode = 6    R = 2
- 5) 5 6 5 4      Mean =  $20 \div 4 = 5$     Med = 5    mode = 5    R = 2
- 6) 6 7 7 7 2 1    Mean =  $30 \div 6 = 5$     Med = 6.5    mode = 7    R = 6

- 7) This table shows how many TVs people have in their homes. Find the mean, median, mode and range from this table.

Number of TVs	Frequency
1	3
2	4
3	2
4	1
<hr style="width: 100px; margin-left: auto;"/>	
10	

$1 \times 3 = 3$   
 $2 \times 4 = 8$   
 $3 \times 2 = 6$   
 $4 \times 1 = 4$   


---

21

Mean =  $\frac{21}{10} = 2.1$     median = 2    Mode = 2    range (TVs) =  $4 - 1 = 3$

- 8) Sally took 5 tests. She scored 45%, 23%, 87%, 62% and 74%.

a) Find the range of Sally's marks.  $87 - 23 = 64\%$ .

b) Find her median mark. 62%

c) Find her mean mark.  $291 \div 5 = 58.2\%$

- 9) Brian took 4 tests. He scored 63%, 58%, 71% and 42%.

a) Find the range of Brian's marks.  $71 - 42 = 29\%$ .

b) Find his median mark.  $\frac{58 + 63}{2} = \frac{121}{2} = 60.5\%$ .

c) Find his mean mark.  $234 \div 4 = 58.5\%$ .

- 10) Use your answers to questions 8 and 9 to answer these questions.

a) Who did better in the tests Brian or Sally? Brian, he had a higher mean.

b) What do their ranges tell you about their test marks?

④

Brian is more consistent, he has a smaller range.

## Averages from a frequency table

1)

Pens	Frequency	P x F	frequency running total
0	4	$0 \times 4 = 0$	4
1	6	$1 \times 6 = 6$	$4 + 6 = 10$
2	7	$2 \times 7 = 14$	$4 + 6 + 7 = 17$
3	5	$3 \times 5 = 15$	$4 + 6 + 7 + 5 = 22$
4	2	$4 \times 2 = 8$	$4 + 6 + 7 + 5 + 2 = 24$
5	1	$5 \times 1 = 5$	25
	25	48	

Find the mean  $48 \div 25 = 1.92$

Find the mode 2 pens

How many pieces of data 25 (number of pieces data + 1)  $\div$  2 =  $\frac{25+1}{2} = 13$

Find the median 13<sup>th</sup> piece of data is a 2

Find the range  $5 - 0 = 5$

2)

Goals	Frequency	G x F	frequency running total
0	7	0	7
1	5	5	12
2	3	6	15
3	6	18	21
4	2	8	23
5	1	5	24
6	1	5	25
	25	47	

Find the mean  $47 \div 25 = 1.88$

Find the mode 0

How many pieces of data 25 (number of pieces data + 1)  $\div$  2 =  $\frac{25+1}{2} = 13$

Find the median 2

Find the range  $6 - 0 = 6$

5

A survey of the length of leaves in a garden

length of leaf in cm	Frequency	midpoint	frequency x midpoint	frequency running total
$0 \leq L < 5$	4	2.5	10	4
$5 \leq L < 10$	5	7.5	37.5	9
$10 \leq L < 15$	6	12.5	75	15
$15 \leq L < 20$	2	17.5	35	17
$20 \leq L < 25$	5	22.5	112.5	22
	22		270	

in a garden was collected. The measurements are in cm

14.2    11.8    21.2    24.0    8.6    6.2    5.7    5.6    5.0    13.9    1.2  
 10.9    19.0    20.0    4.6    2.6    23.0    1.5    10.0    22.3    11.0    18.4

Complete the frequency section of the table

What is the modal group?  $10 \leq L < 15$

Find an estimate of the mean  $270 \div 22 = 12.3 \text{ cm}$

Which group contains the median?  $\frac{11^{\text{th}} + 12^{\text{th}}}{2}$

$11^{\text{th}}$  and  $12^{\text{th}}$  both in the group  $10 \leq L < 15$

# Averages review

## A set of numbers

2, 7, 8, 7, 3

mean  $27 \div 5 = 5.4$

median 7

mode 7

range  $8 - 2 = 6$

2, 5, 5, 3, 5, 4

mean  $24 \div 6 = 4$

median  $\frac{3+4}{2} = 3.5$

mode 5

range  $5 - 2 = 3$

## A frequency table

pets	frequency	
0	3	0
1	6	6
2	5	10
3	3	9
4	1	4

18      29

mean  $29 \div 18 = 1.6$

median  $\frac{1+2}{2} = 1.5$

mode 1

range  $4 - 0 = 4$

## A grouped frequency table

height	frequency	midpoint	mid x freq
$0 \leq h < 10$	4	5	20
$10 \leq h < 20$	7	15	105
$20 \leq h < 30$	6	25	150
$30 \leq h < 40$	2	35	70
$40 \leq h < 50$	1	45	45

20

390

estimate of the mean  $390 \div 20 = 19.5$

modal group  $10 \leq h < 20$

group containing the median  $10 \leq h < 20$

## Adding an extra piece of data

John has taken 4 tests, his mean score so far is 7 out of 10. In his 5th test he scored 2 out of 10. What is his mean score now?

Find the total of John's 4 tests.  $4 \times 7 = 28$  Add the 5th score  $28 + 2 = 30$  Mean =  $\frac{30}{5} = 6$

## Is the answer sensible?

TVs	Frequency
1	2
2	5
3	2

This survey shows the number of TVs per house.

Sally calculated that the mean number of TVs per house is 6.

Is this sensible? No the mean must be between 1 and 3, the least and most number of TVs

## Is it sensible to use the mean?

These are the ages of a group of students and their teacher. 11, 12, 11, 12, 11, 12, 12, 11, 12, 45

Is the mean a good average to use (explain your answer)? NO, because of the teacher.

Which average would be better in this example? median.

7